Assuring Autonomy in Contested Environments Attack-Resilient Design



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Attack Resilient Design

- Distributed methods for attack-detection & identification (ADI) and security-aware mission planning by exploiting dynamics of the environment and agents, as well as our knowledge of the expected mission evolution
- Develop a platform-aware attack-resilient architecture integrating the control and estimation techniques for resource-constrained autonomous systems
- Develop methods to assure desired QoC despite communication and computation limitations (optimal balance between QoC and security guarantees)
- Investigate MDPs, PTAs, and stochastic hybrid automata (SHAs, to model the interaction between the IDS and the controller/environment



Vehicle Trajectory Following



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Attack-Resilient Design of Autonomous Systems Attacks on Autonomous Control

- 1. Sensor attacks
 - The attacker can arbitrarily change sensor measurements
- 2. Actuator attacks
 - The attacker can arbitrarily change actuator values
- 3. Communication attacks
 - The attacker can change messages between sensors and controllers, and messages between controllers and actuators.
- 4. Controller attacks
 - The attacker can change the controllers' parameters, resources (e.g., execution model) or even the controllers' code.





Security-Aware Design of Autonomous Systems

- Physical world abides by the laws of physics!
- Physical interfaces introduce new attack vectors!

• How can we exploit *limited* knowledge of laws of physics (system model) for control and attack detection/identification

- Attack-Resilient design with *uncertainty, resource/platform constraints,* as well as varying (especially high) levels of autonomy
 - How much can the attacker exploit modeling limitation?
 - How can we effectively exploit physics to improve guarantees in the presence of attacks?

Security-Aware Control for Autonomous Systems





Our Goal: Add resiliency to controls across different/all levels of control stack



- Attack-resilient control of Cyber-Physical Systems
 - Idea: Design attack-resilient state estimators

- Initially required an accurate LTI system model
 - Fawzi *et al.* 2012
 - Pasqualetti *et al.* 2013



 If the number of attacked sensors is below a threshold, state can be reconstructed from a history of sensor readings [Fawzi *et al.* 2012]
 Also identifies the sensors under attack

Modeling attacks on sensors and *actuators*

- Consider an LTI system
- $-\mathbf{x}_k \in \mathbb{R}^n$ plant's state at time k
- $-\mathbf{u}_k \in \mathbb{R}^m$ plant input at time k
- $-\mathbf{y}_k \in \mathbb{R}^p$ plant output
 - state information is availably only via sensors measurements
 - $\mathcal{S} = \{s_1, s_2, \dots, s_p\}$

- Attacks on sensors in $\mathcal{K} = \{s_{i_1}, \dots, s_{i_d}\} \subseteq S$
- modeled with attack vector \mathbf{e}_k
- $-\mathbf{e}_{k,i} \neq 0 \iff \text{sensor } s_i \text{ is under attack at time } k$











Problem Description

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- We consider an LTI system, with state $\mathbf{x} \in \mathbb{R}^n$ and output $\mathbf{y} \in \mathbb{R}^p$ measurements from the set of sensors $\mathcal{S}=\{s_1,s_2,\ldots,s_p\}$

$$egin{aligned} \mathbf{x}_{k+1} &= \mathbf{A}\mathbf{x}_k \ \mathbf{y}_k &= \mathbf{C}\mathbf{x}_k + \mathbf{w}_k + \mathbf{e}_k \end{aligned}$$

— bounded size noise
$$|\mathbf{w}_k| \leq \delta_{w_k}$$

— sparse attack vector $\mathbf{e} \in \mathbb{R}^p$ captures attacks on a subset of sensors $\mathcal{K} = \{s_{i_1}, s_{i_2}, \dots, s_{i_q}\} \subseteq \mathcal{S}$

$\mathcal{K} = \{s_2, s_5\}$	
	[0]
	1.7
$\mathbf{e}_k =$	0
	0
	9-

• Goal: *Reconstruction* of the initial system state \mathbf{x}_0 from a set of *N* output observations $\mathbf{y}_0, \mathbf{y}_1, \dots, \mathbf{y}_{N-1}$

$$\mathbf{y}_k = \mathbf{C}\mathbf{A}^k\mathbf{x}_0 + \mathbf{e}_k + \mathbf{w}_k$$

• System evolution observed via a single sensor

$$ilde{\mathbf{y}}_i = egin{bmatrix} \mathbf{y}_{0,i} \ \mathbf{y}_{1,i} \ dots \ \mathbf{y}_{N-1,i} \end{bmatrix} \in \mathbb{R}^N \qquad ilde{\mathbf{e}}_i = egin{bmatrix} \mathbf{e}_{0,i} \ \mathbf{e}_{1,i} \ dots \ \mathbf{e}_{1,i} \ dots \ \mathbf{e}_{1,i} \end{bmatrix} \in \mathbb{R}^N \qquad ilde{\mathbf{w}}_i = egin{bmatrix} \mathbf{w}_{0,i} \ \mathbf{w}_{1,i} \ dots \ \mathbf{w}_{1,i} \ dots \ \mathbf{w}_{N-1,i} \end{bmatrix} \in \mathbb{R}^N \qquad 1 \leq i \leq p$$

$$ilde{\mathbf{y}}_i = \mathbf{O}_i \mathbf{x}_0 + ilde{\mathbf{e}}_i + ilde{\mathbf{w}}_i$$

• System evolution observed from all sensors

$$ilde{\mathbf{y}} = egin{bmatrix} ilde{\mathbf{y}}_1 \\ dots \\ ilde{\mathbf{y}}_p \end{bmatrix}, ilde{\mathbf{e}} = egin{bmatrix} ilde{\mathbf{e}}_1 \\ dots \\ ilde{\mathbf{e}}_p \end{bmatrix}, ilde{\mathbf{w}} = egin{bmatrix} ilde{\mathbf{w}}_1 \\ dots \\ ilde{\mathbf{w}}_p \end{bmatrix}, extbf{O} = egin{bmatrix} olde{\mathbf{O}}_1 \\ dots \\ olde{\mathbf{O}}_p \end{bmatrix}$$

 $\tilde{\mathbf{y}} = \mathbf{O}\mathbf{x}_0 + \tilde{\mathbf{e}} + \tilde{\mathbf{w}}$

$$\begin{bmatrix} P_{\{s_i\}} \mathbf{C} \\ P_{\{s_i\}} \mathbf{C} \mathbf{A} \\ \vdots \end{bmatrix} \qquad \mathbf{O}_{\mathcal{K}} = \begin{bmatrix} \mathbf{O}_{s_{i_1}} \\ \mathbf{O}_{s_{i_2}} \\ \vdots \end{bmatrix}$$

$$\mathbf{O}_{s_i} = \begin{bmatrix} P_{\{s_i\}} \mathbf{C} \\ P_{\{s_i\}} \mathbf{C} \mathbf{A} \\ \vdots \\ P_{\{s_i\}} \mathbf{C} \mathbf{A}^{N-1} \end{bmatrix} \qquad \mathbf{O}_{\mathcal{K}} = \begin{bmatrix} \mathbf{O}_{s_{i_1}} \\ \mathbf{O}_{s_{i_2}} \\ \vdots \\ \mathbf{O}_{s_{i_{|\mathcal{K}|}}} \end{bmatrix}$$



• System evolution observed via a single sensor

• System evolution observed from all sensors

$$egin{aligned} ilde{\mathbf{y}}_{i,i} \ dots \ \mathbf{y}_{1,i} \ dots \ \mathbf{y}_{N-1,i} \end{aligned} &\in \mathbb{R}^N & ilde{\mathbf{e}}_i = egin{bmatrix} \mathbf{e}_{0,i} \ \mathbf{e}_{1,i} \ dots \ \mathbf{e}_{1,i} \ dots \ \mathbf{e}_{1,i} \end{aligned} &\in \mathbb{R}^N & ilde{\mathbf{w}}_i = egin{bmatrix} \mathbf{w}_{0,i} \ \mathbf{w}_{1,i} \ dots \ \mathbf{w}_{1,i} \ dots \ \mathbf{w}_{N-1,i} \end{aligned} &\in \mathbb{R}^N & 1 \leq i \leq p \end{aligned}$$

$$ilde{\mathbf{y}}_i = \mathbf{O}_i \mathbf{x}_0 + ilde{\mathbf{e}}_i + ilde{\mathbf{w}}_i$$

$$\mathbf{O}_{s_i} = \begin{bmatrix} P_{\{s_i\}} \mathbf{C} \\ P_{\{s_i\}} \mathbf{C} \mathbf{A} \\ \vdots \\ P_{\{s_i\}} \mathbf{C} \mathbf{A}^{N-1} \end{bmatrix} \qquad \mathbf{O}_{\mathcal{K}} = \begin{bmatrix} \mathbf{O}_{s_{i_1}} \\ \mathbf{O}_{s_{i_2}} \\ \vdots \\ \mathbf{O}_{s_{i_{|\mathcal{K}|}}} \end{bmatrix}$$



Attack-Resilient State Estimation for Noisy Dynamical Systems

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- Consider an initial state \mathbf{x}_0 and attack vectors from $\mathbf{ ilde{e}}$

$$egin{aligned} P_0 : & \min_{ ilde{\mathbf{e}}, \mathbf{x}} \| ilde{\mathbf{e}} \|_{l_2, l_0} \ s. t. & ilde{\mathbf{y}} - \mathbf{O} \mathbf{x}_0 - ilde{\mathbf{e}} = \mathbf{0} \end{aligned}$$

- Goal: guarantees for $P_{0,\omega}$ and $P_{1,\omega}$ based estimators
 - Bounds on the state estimation errors
 - Sound attacked sensor identification

$$egin{aligned} P_{0,\omega}:&\min_{ ilde{\mathbf{e}},\mathbf{x}}\| ilde{\mathbf{e}}\|_{l_2,l_0}\ s.\,t.& ilde{\mathbf{y}}-\mathbf{O}\ \mathbf{x}_0- ilde{\mathbf{e}}= ilde{\mathbf{w}}\ ilde{\mathbf{w}}\in\Omega \end{aligned}$$
 $egin{aligned} P_{1,\omega}:&\min_{ ilde{\mathbf{e}},\mathbf{x}}\| ilde{\mathbf{e}}\|_{l_2,l_1}\ s.\,t.& ilde{\mathbf{y}}-\mathbf{O}\ \mathbf{x}_0- ilde{\mathbf{e}}= ilde{\mathbf{w}}\ ilde{\mathbf{w}}\in\Omega \end{aligned}$

[ICCPS'14 – Best paper award, CDC15, IEEE CSM'17, IEEE TCNS'17]

Performance Guarantees for $P_{0,\omega}$ Estimator



$$\begin{aligned} (\mathbf{x}_{l_0,\omega}, \tilde{\mathbf{e}}^{l_0}) &= \arg\min P_{0,\omega}, \quad q_{0,\omega} = \|\tilde{\mathbf{e}}^{l_0}\|_{l_2,l_0} \\ \Delta \mathbf{x}^{l_0} &= \mathbf{x}_{l_0,\omega} - \mathbf{x}_0, \quad \Delta \tilde{\mathbf{e}}^{l_0} = \tilde{\mathbf{e}}^{l_0} - \tilde{\mathbf{e}}^* \end{aligned}$$

- Definition [Shoukry *et al.*, 2013]: An LTI system is *s*-sparse observable if for every set K ⊆ S of size *s*, the pair (A, P_{K^C}C) is observable
- Lemma: q_{max} is equal to the maximal *s* for which the system is 2*s*-sparse observable

• Theorem: If $q \leq q_{max}$ sensors have been attacked, then

$$\|\Delta \mathbf{x}^{l_0}\|_{l_2} \leq 2 \cdot \max_{\substack{\mathcal{R} \subset S, \ |\mathcal{R}| = p-2q_{max}}} \left(\|\mathbf{O}_\mathcal{R}^\dagger\|_{l_2} \cdot \max_{\mathbf{ ilde w}_\mathcal{R} \in \Omega_\mathcal{R}} \|\mathbf{ ilde w}_\mathcal{R}\|_{l_2}
ight)$$

Performance Guarantees for $P_{1,\omega}$ Estimator

$$(\mathbf{x}_{l_1,\omega}, \tilde{\mathbf{e}}^{l_1}) = \arg \min P_{1,\omega}$$
$$\Delta \mathbf{x}^{l_1} = \mathbf{x}_{l_1,\omega} - \mathbf{x}_0, \quad \Delta \tilde{\mathbf{e}}^{l_1} = \tilde{\mathbf{e}}^{l_1} - \tilde{\mathbf{e}}^*$$

• Theorem: If q sensors from the set $\mathcal{K} \subseteq \mathcal{S}$ have been attacked, then

$$\sum_{\mathbf{a}_i \in \mathcal{K}^\complement} \| \mathbf{O}_i \Delta \mathbf{x}^{l_1} \|_{l_2} \leq \sum_{s_i \in \mathcal{K}} \| \mathbf{O}_i \Delta \mathbf{x}^{l_1} \|_{l_2} + 2 \sigma_\Omega$$

where

$$\sigma_\Omega = \max_{ ilde{\mathbf{w}}\in\Omega} \| ilde{\mathbf{w}} \|_{l_2,l_1}$$

• Proposition: If $P_{1,\omega}$ correctly estimates the state for a noiseless system, then the error is either zero or for all $\mathcal{K} \subseteq \mathcal{S}$ with q elements

$$\sum_{s_i \in \mathcal{K}} \| \mathbf{O}_i \Delta \mathbf{x}^{l_1} \|_{l_2} < \sum_{s_i \in \mathcal{K}^\complement} \| \mathbf{O}_i \Delta \mathbf{x}^{l_1} \|_{l_2} \leq \sum_{s_i \in \mathcal{K}} \| \mathbf{O}_i \Delta \mathbf{x}^{l_1} \|_{l_2} + 2\sigma_\Omega$$

Performance Guarantees for $P_{1,\omega}$ Estimator

$$(\mathbf{x}_{l_1,\omega}, \tilde{\mathbf{e}}^{l_1}) = \arg \min P_{1,\omega}$$
$$\Delta \mathbf{x}^{l_1} = \mathbf{x}_{l_1,\omega} - \mathbf{x}_0, \quad \Delta \tilde{\mathbf{e}}^{l_1} = \tilde{\mathbf{e}}^{l_1} - \tilde{\mathbf{e}}^*$$

• Theorem: Suppose that for all $\mathcal{K} \subseteq \mathcal{S}$ with q elements

$$\mathbf{O}_{\mathcal{K}^\complement}^T \mathbf{O}_{\mathcal{K}^\complement} - qN^2 \mathbf{O}_{\mathcal{K}}^T \mathbf{O}_{\mathcal{K}} \succeq \lambda \mathbf{I}_n$$

for some $\lambda > 0\,$. Then if most q sensors are compromised it holds

$$\|\Delta \mathbf{x}^{l_1}\|_{l_2} \leq rac{2\sqrt{N}\sigma_\Omega}{\lambda} \cdot \max_{\mathcal{K} \subset \mathcal{S}, |\mathcal{K}|=q} (\|\mathbf{O}_{\mathcal{K}^\complement}\|_{l_2} + \sqrt{q}N\|\mathbf{O}_{\mathcal{K}}\|_{l_2})$$

• For N=1, a static state estimation problem $\mathbf{y} = \mathbf{C}\mathbf{X} + \mathbf{e} + \mathbf{w}$

- The above condition is not as conservative

One candidate

$$\mathbb{I}(ilde{\mathbf{e}}_i^{l_t}
eq \mathbf{0})$$

Thus, we use the state estimation guarantees

$$Attacked^{l_t}(s_i) = \mathbb{I}(\| ilde{\mathbf{e}}_i^{l_t}\|_{l_2} > D_i^{ ilde{\mathbf{e}}^{l_t}}), \qquad i=1,\ldots,p.$$

- Sound
- Identifies all attack vectors that satisfy $\|\tilde{\mathbf{e}}_i^*\|_{l_2} > 2D_i^{\tilde{\mathbf{e}}^{l_t}}$

Attack-Resilient Cruise Control Demo





Attack-resilient state estimator for American Built Car

- CarSim Simulation
- In-Car Implementation





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Attack-resilient state estimator for an American Built Car





Security-Aware Control for Autonomous Systems





Our Goal: Add resiliency to controls across different/all levels of control stack

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- Guarantees for complex system dynamics
 - Requirements from attack-resilient supervisory control (IEEE TAC'19, CDC'19a, CDC'19b)
 - Probabilistic sensor models Connection to privacy guarantees
- Combining with data-driven methods for attack-detection and identification
- How to add context-based sensing (IEEE TAC 2018)
- Using GPS high variance and bias
- Camera-based landmark recognition



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- Available actuation signals are not only used to optimally control physical process, but to also increase confidence that the system has not been compromised
 - For replay attack detection [Automatika'18]
- Challenge: resiliency and performance
 objective may conflict
- Proposed work: derive framework for optimal use of active monitoring that balances performance and attack detection requirements
- Nonlinearity is our friend!









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Information inside this box is oftentimes unknown, i.e., hidden

Off-the-shelf model checkers do NOT support hidden variables Strategies CANNOT be synthesized based on hidden information

Private Variables Representation



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Delayed Actions Representation [CAV19]



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Proper simulation [CAV19]





Bisimulation allows model checking and strategy synthesis using standard tools





Case Study | Results







 Develop planning methods that will improve attack-detection guarantees by allowing the deployed intrusion detection system to interact with the controller and the rest of the system

How to model such interactions? – MDPs, PTAs, SHAs

- Optimization based on solving stochastic games
 - How to incorporate learning?
 - How to incorporate formal guarantees?



[ICRA'19, iEEE THMS'19]





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Security-Aware Control for Autonomous Systems Are we done?



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Our Goal: Add resiliency to controls across different/all levels of control stack

Security-Aware Control for Autonomous Systems Are we done? No – conservative assumptions!





Our Goal: Add resiliency to controls across different/all levels of control stack









$\mathbf{x}_{k+1} = \mathbf{A}\mathbf{x}_k + \mathbf{B}\mathbf{u}_k + \mathbf{w}_k$	$supp(\mathbf{a}_k) = \mathcal{K}$
$\mathbf{y}_k = \mathbf{C}\mathbf{x}_k + \mathbf{a}_k + \mathbf{v}_k$	$\mathbf{a}_{k,i}=0, \forall i\in\mathcal{K}^{0}$

Theorem 1 [1,2,3]:

A system presented above is perfectly attackable if and only if the matrix **A** is unstable, and at least one eigenvector **v** corresponding to an unstable mode satisfies $supp(\mathbf{Cv}) \subseteq \mathcal{K}$ and **v** is a reachable state of the dynamic system.

Physical detectors cannot always protect us from an intelligent attacker... Can data authentication help?

[1] Y. Mo and B. Sinopoli, "False data injection attacks in control systems," in First Workshop on Secure Control Systems, 2010
 [2] C. Kwon, W. Liu, and I. Hwang, "Analysis and design of stealthy cyber attacks on unmanned aerial systems", Journal of Aerospace Information Systems, 1(8), 2014

[3] I. Jovanov and M. Pajic, "Relaxing Integrity Requirements for Attack-Resilient Cyber-Physical Systems", IEEE Trans. on Automatic Control, 2019

Definition 2: Intermittent data integrity enforcement policy (μ, f, L) , where $\mu = \{t_k\}_{k=0}^{\infty}$, such that for all k > 0, $t_{k-1} < t_k$ and $L = \sup_{k>0} t_k - t_{k-1}$ ensures that

$$\mathbf{a}_{t_k} = \mathbf{a}_{t_k+1} = \dots = \mathbf{a}_{t_k+f-1} = \mathbf{0}, \forall k \ge 0$$

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Definition: Intermittent data integrity enforcement policy (μ, f, L) , where $\mu = \{t_k\}_{k=0}^{\infty}$, such that for all k > 0, $t_{k-1} < t_k$ and $L = \sup_{k>0} t_k - t_{k-1}$ ensures that

$$\mathbf{a}_{t_k} = \mathbf{a}_{t_k+1} = \dots = \mathbf{a}_{t_k+f-1} = \mathbf{0}, \forall k \ge 0$$

Theorem: A system Σ with a global data integrity policy (μ, f, L) , where $f = \min(nullity(\mathbf{C}) + 1, q_{un})$

and q_{un} is the number of distinct unstable eigenvalues of **A**, is not perfectly attackable.

^[1] I. Jovanov and M. Pajic, "Sporadic Data Integrity for Secure State Estimation", IEEE Conference on Decision and Control (CDC), 2017

^[2] I. Jovanov, and M. Pajic, "Secure State Estimation with Cumulative Message Authentication", IEEE Conference on Decision and Control (CDC), 2018

^[3] I. Jovanov and M. Pajic, Relaxing Integrity Requirements for Resilient Control Systems, (2017). IEEE Transactions on Automatic Control, 2019

State Estimation Error In the Presence of Stealthy Attacks



Reachable region of the state estimation error under attack $^{[1,2,3]}$

$$\mathcal{R}[k] = \left\{ \boldsymbol{e} \in \mathbb{R}^{\boldsymbol{n}} \middle| \begin{array}{l} \boldsymbol{e} \boldsymbol{e}^{\mathrm{T}} \leq E[\boldsymbol{e}^{a}[k]] E[\boldsymbol{e}^{a}[k]]^{\mathrm{T}} + \gamma Cov(\boldsymbol{e}_{k}^{a}) \\ \boldsymbol{e}^{a}[k] = \boldsymbol{e}_{k}^{a}(\boldsymbol{a}_{1...k}), \boldsymbol{a}_{1...k} \in \mathcal{A}_{k} \end{array} \right\}$$

 $\mathbf{a}_{1\dots k} = [\mathbf{a}[1]^{\mathrm{T}} \dots \mathbf{a}[k]^{\mathrm{T}}]^{\mathrm{T}}$ \mathcal{A}_k is the set of all stealthy attacks

 $e_k^a(\mathbf{a}_{1...k})$ is the estimation error evolution due to attack $\mathbf{a}_{1...k}$



---k=1 ---k=3 ---k=4 w/o int. enf. ---k=4 w/ int. enf.



Integrity enforcement policy ensures attacker's influence is zeroed at enforcement points

Data integrity enforcement policy (μ, l) where $\mu = \{t_k\}_{k=0}^{\infty}$, with $t_{k-1} < t_k, \forall k > 0$ and $l = \sup_{k>0} t_k - t_{k-1}$ ensures that $\mathbf{a}_{1...k} = 0, \forall k \ge 0$

This means that at points of authentication $y_i^{net,a}[k] = y_i^a[k]$



---k=1 ---k=2 ---k=3 ---k=4 w/o int. enf. ---k=4 w/ int. enf.



Relaxing Integrity Guarantees for Secure Vehicle Platooning

Ilija Jovanov, Vuk Lesi, Miroslav Pajic Duke University

Secure Vehicle Platooning With Intermittent Integrity Guarantees





System Performance Metric Quality-of-Control (QoC) under Attack

Evolution of the state-estimation error due to attack is a sound performance metric

$$\mathcal{J}(l) = \sup\{\|\boldsymbol{e}^a\|_2 | \boldsymbol{e}^a \in \mathcal{R}^l\} \qquad \mathcal{R}^l = \bigcup_{k=0}^{\infty} \mathcal{R}^l[k]$$

where $\mathcal{R}^{l}[k]$ denotes $\mathcal{R}[k]$ computed over all integrity enforcement policies with parameter l









Three Scheduling Problems





- ECUs are the bottleneck [ACM TECS/EMSOFT 17] Best Paper Award!
- Network is the bottleneck [RTSS 17]
- Both ECU time and network bandwidth are a concern ACM TCPS*

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- Goal: Derive distributed, event-based resilient control/estimation for cases when only intermittent communication between agents can be achieved
- When such communication should occur, how often, and between which agents?
- How we can opportunistically use available communication links to increase mission resilience against attacks.
- These requirements will be used as part of the design specifications for intermittent wireless communication in RT3
- Rich security models
 - Cumulative authentication
 - Forgery attacks
 - Probabilistic guarantees



Thank you











