

# Structural Alignment in Worst-case Security Analysis and Multi-agent Design



Washington Garcia (UF)

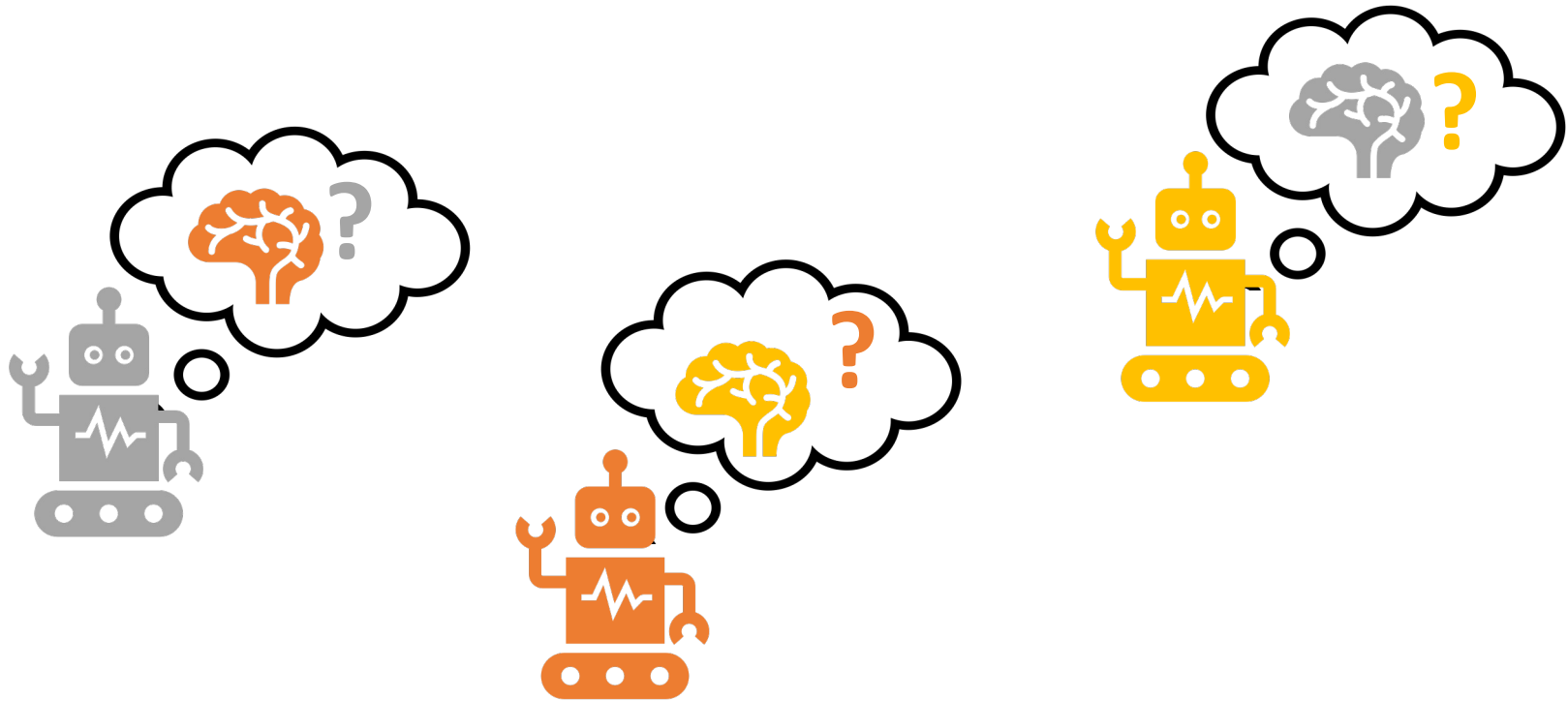
Kevin Butler (UF)

Pin-Yu Chen (IBM)

Somesh Jha (UW)

Scott Clouse (AFRL/ACT3)

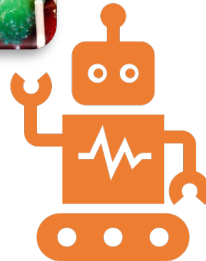
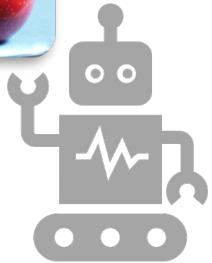
Entities in a multi-agent system must be aware of their surroundings, but also the *representational structure* of their counterparts. This can bolster situational awareness:





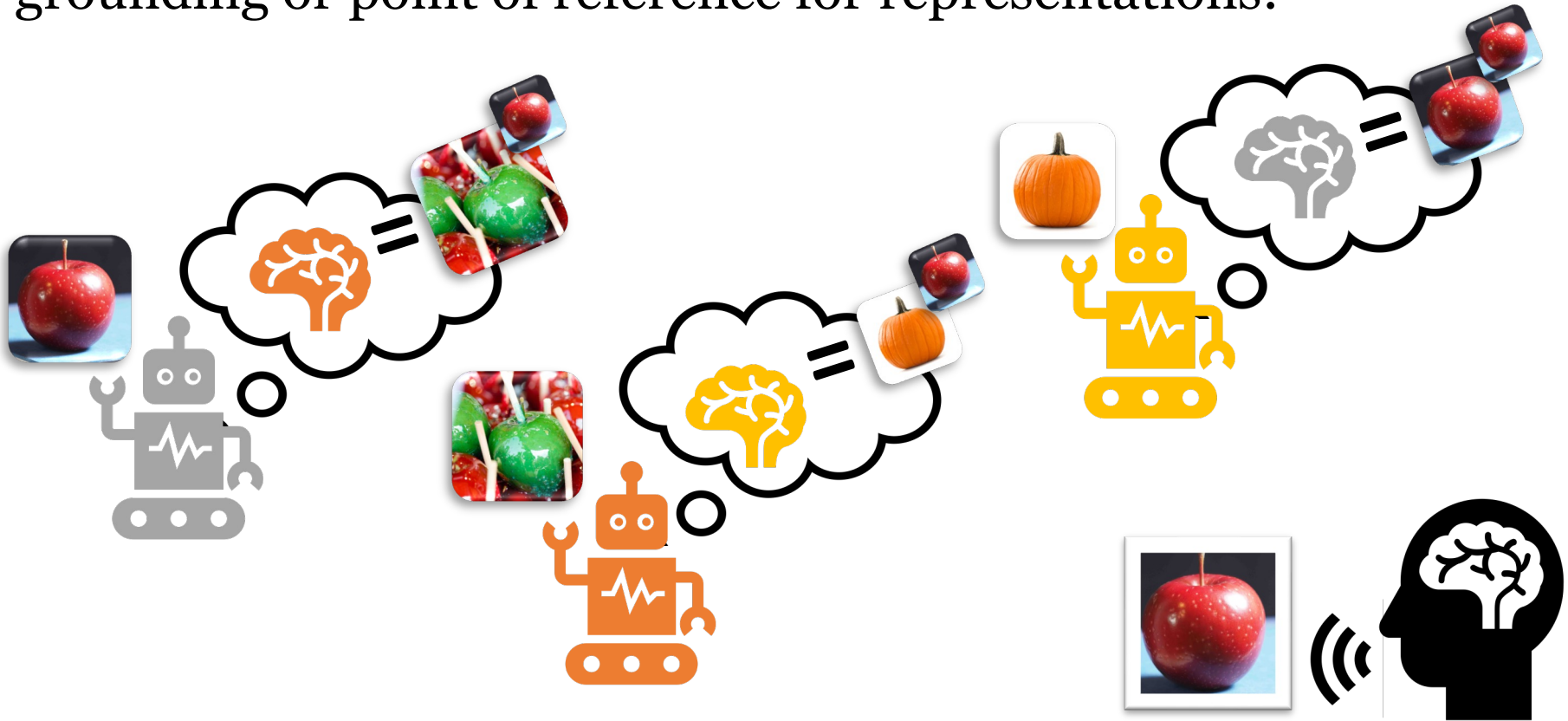
What is a good yardstick for representations?

A “human-in-the-loop” or proxy thereof can provide a grounding or point of reference for representations:



What is a good yardstick for representations?

A “human-in-the-loop” or proxy thereof can provide a grounding or point of reference for representations:





Two main questions:

1. Is agent concept resolution possible from an **adversary's** perspective? What's the worst-case security analysis?
2. It isn't always realistic to have a human-in-the-loop, or fine-grained data labels. What are ways around this?

A1: Expansion of our previous hard-label paper, in submission to IEEE SaTML 2023.

A2: Presented initial idea @ NAACL 2022. Introduced expansion during previous meeting. Then worked on it as part of AFRL 2022 internship.



Two main questions:

1. Is agent concept resolution possible from an **adversary's** perspective? What's the worst-case security analysis?
2. It isn't always realistic to have a human-in-the-loop, or fine-grained data labels. What are ways around this?

A1: Expansion of our previous hard-label paper, in submission to IEEE SaTML 2023.

A2: We presented an initial idea @ NAACL 2022. Introduced expansion during previous meeting. Then worked on it as part of AFRL 2022 internship.

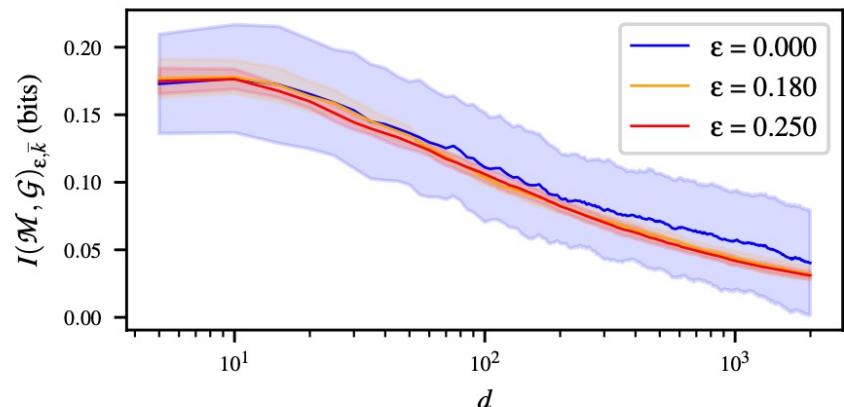
Assumptions:

1. Agent data lives on a low-dimensional manifold
2. The distribution of data points ( $\mathcal{M}$ ), true gradients ( $\mathcal{G}$ ), and ZO gradient estimates form a Markov chain:

$$\mathcal{M} \rightarrow \mathcal{G} \rightarrow \tilde{\mathcal{G}}$$

We showed previously that manifold-gradient *mutual information* can be modeled as a function of data dimension:

$$I(\mathcal{M}; \mathcal{G})_{\epsilon, k} = 2 \int_{\mathcal{M}^+} p(1, \mathbf{x}^+) \log\left(\frac{p(1, \mathbf{x}^+)}{p_{\mathcal{G}}(1)p_{\mathcal{M}}(\mathbf{x}^+)}\right) d\mathbf{x}^+ \\ + 2 \int_{\mathcal{M}^+} p(-1, \mathbf{x}^+) \log\left(\frac{p(-1, \mathbf{x}^+)}{p_{\mathcal{G}}(-1)p_{\mathcal{M}}(\mathbf{x}^+)}\right) d\mathbf{x}^+.$$



In practice, *does the Markov chain (MC) exist?*

First, show that the MC can be modeled by a zeroth-order (i.e., hard-label) adversary through two algorithms.

Local step neighborhood analysis (Algorithm 1):

Build local neighborhood from ZO queries as Gaussian process (GP) →

Use queries to train linear model of decision boundary. →

---

**Algorithm 1:** Local Markov chain step (MC\_step)

---

**Input:** Hard-label Gaussian process (GP), LIME  
kernel width  $k$

**Output:** Sample feature coefficients  $W \in \mathbb{R}^d$  and their  
quality score  $R^2 \in \mathbb{R}$ , GP result (res)

```

1 initialize LIME Ridge regression trainer (LIME) [31]
2 /* Execute GP to collect samples */
3  $X, Y, res \leftarrow GP()$ 

4  $f_W \leftarrow LIME(X, Y, k)$ 
5  $R^2 \leftarrow f_W(X)$ 
6 return  $W, R^2, res$ 

```

---



In practice, *does the Markov chain (MC) exist?*

First, show that the MC can be modeled by a zeroth-order (i.e., hard-label) adversary through two algorithms.

Local step neighborhood analysis (Algorithm 1):

---

**Algorithm 1:** Local Markov chain step (MC\_step)

---

Build local neighborhood from ZO queries as Gaussian process (GP)

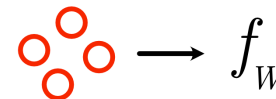
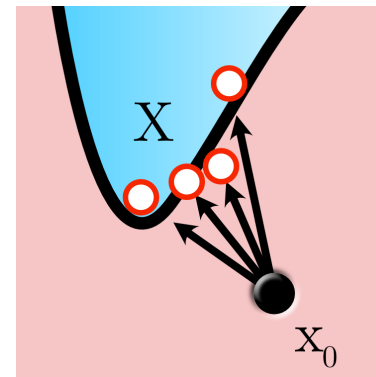


1  
2  
3

Use queries to train linear model of decision boundary.



4  
5  
6





Using Algorithm 1 to model local ZO queries, we can model the whole-attack agent Markov chain through Bayesian optimization (OptiLIME).

---

**Algorithm 2:** Markov chain probing of hard-label attack

---

Call Algorithm 1 →

Call Algorithm 1 →

Get “quality” of MC models ( $R^2$ ) →

```

1 GP := (init,  $\mathbf{x}_0$ )
2 kernel width  $k \leftarrow$  OptiLIME(MC_step, GP)
3 /* Initialize through MC_step */
4  $W_{init}, R^2, \mathbf{x} \leftarrow$  MC_step(GP,  $k$ )
5 for  $i := 1$  to  $n$  do Hard-label attack loop
6   GP  $\leftarrow$  (approximate_gradient,  $\mathbf{x}$ )
7    $k \leftarrow$  OptiLIME(MC_step, GP,  $\mathbf{x}'$ )
8   /* Approximate through MC_step */
9    $W_{\hat{\mathbf{g}}_i}, R^2, \boldsymbol{\theta} \leftarrow$  MC_step(GP,  $k$ )
10  Update  $\mathbf{x}$  from  $\boldsymbol{\theta}$  using attack formulation
11 end
12 return  $\mathbf{x}, \{W_{init}, W_{\hat{\mathbf{g}}_1}, \dots, W_{\hat{\mathbf{g}}_n}\},$ 
    $\{R^2_{init}, R^2_{\hat{\mathbf{g}}_1}, \dots, R^2_{\hat{\mathbf{g}}_n}\}$ 

```

---

Using Algorithm 1 to model local ZO queries, we can model the whole-attack agent Markov chain through Bayesian optimization (OptiLIME).

---

**Algorithm 2:** Markov chain probing of hard-label attack



---

Call Algorithm 1 →

Call Algorithm 1 →

Get “quality” of MC models ( $R^2$ ) →

```

1 GP := (init,  $\mathbf{x}_0$ )
2
3  →  $f_W$  →  $R_{init}^2$ 
4
5 for  $i := 1$  to  $n$  do Hard-label attack loop
6   GP ← (approximate_gradient,  $\mathbf{x}$ )
7
8    →  $f_W$  →  $R_{\hat{\mathbf{g}}_i}^2$ 
9
10  Update  $\mathbf{x}$  from  $\theta$  using attack formulation
11 end
12 return  $\mathbf{x}$ ,  $\{W_{init}, W_{\hat{\mathbf{g}}_1}, \dots, W_{\hat{\mathbf{g}}_n}\}$ ,
     $\{R_{init}^2, R_{\hat{\mathbf{g}}_1}^2, \dots, R_{\hat{\mathbf{g}}_n}^2\}$ 

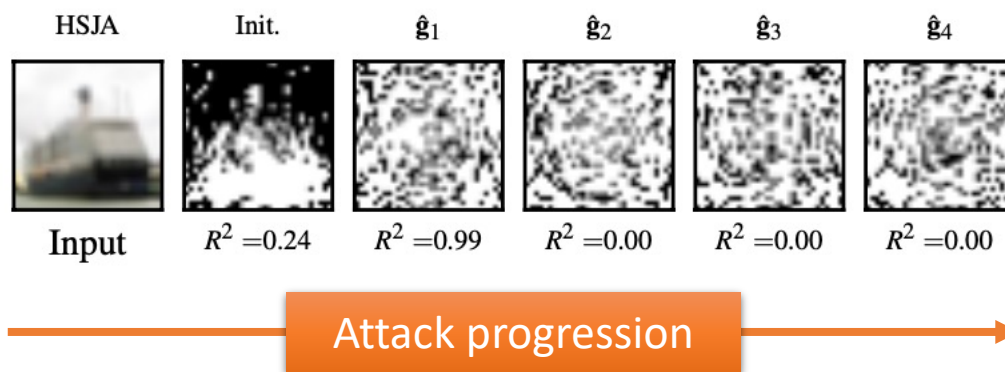
```

---

Using (average)  $R^2$  score of local models, we can answer the following:

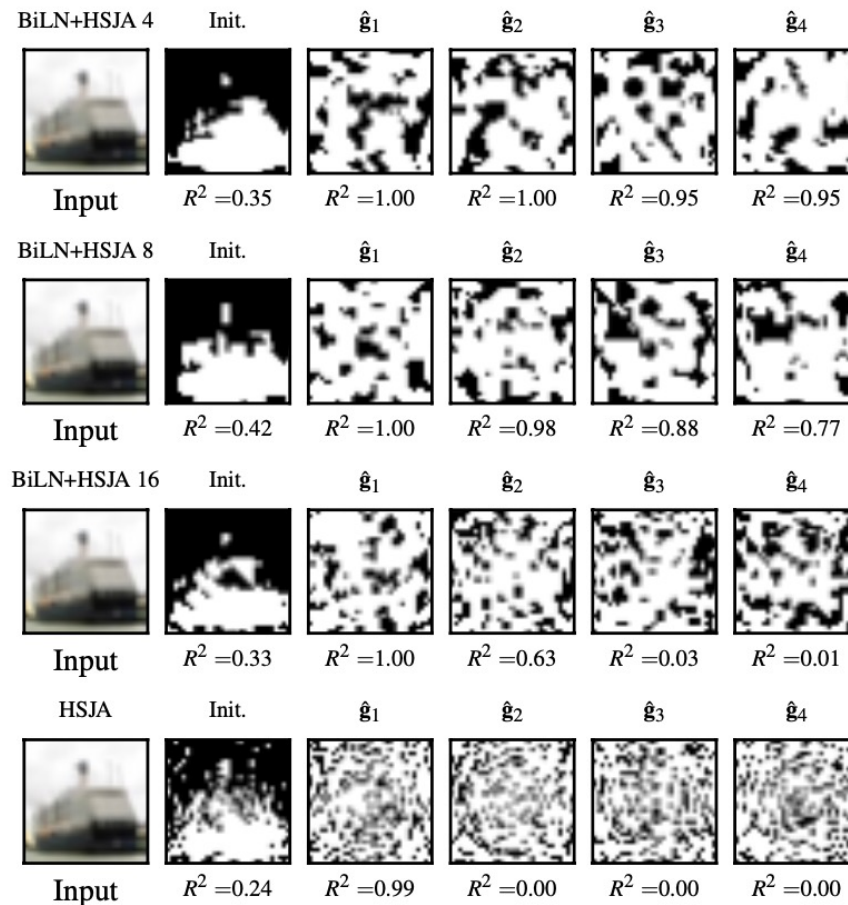
1. Are hard-label queries sufficient to model the model's semantic structure in the query neighborhood?
2. Does dimension-reduction influence our structural knowledge?

A1. Yes:

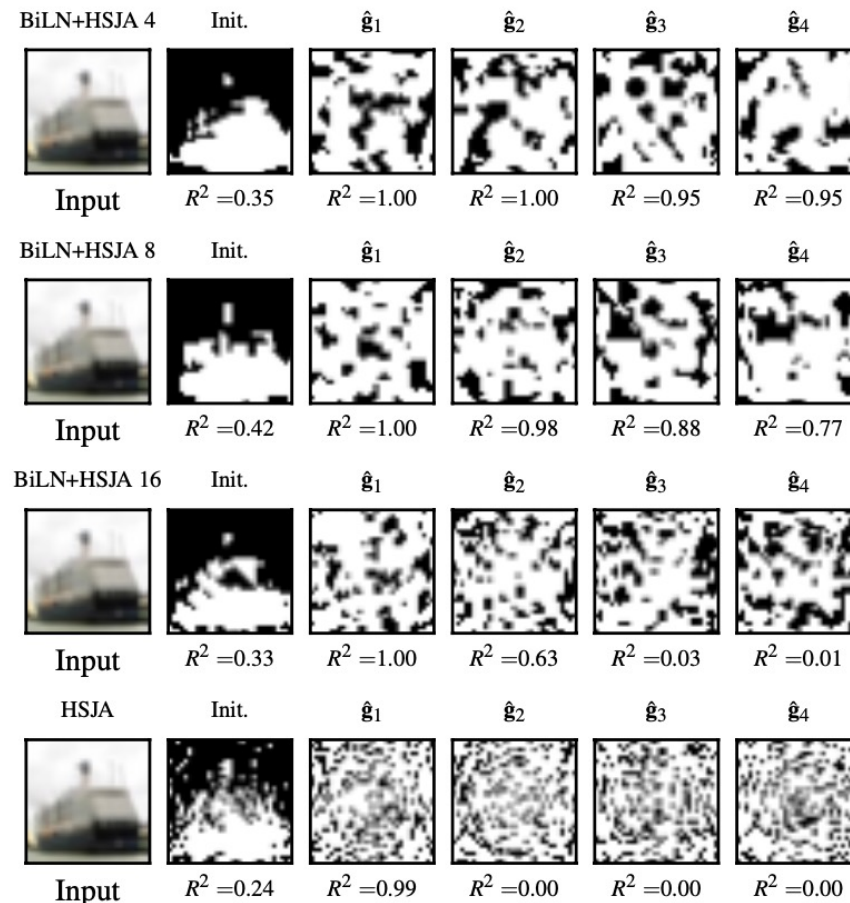
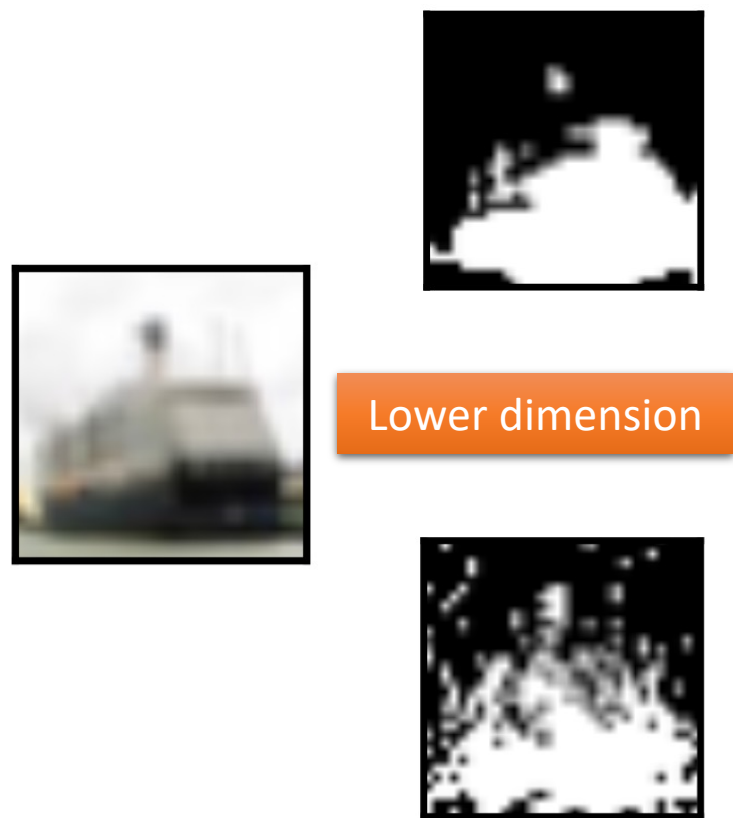


## A2. Dimension-reduction leads to finer-grained structural information:

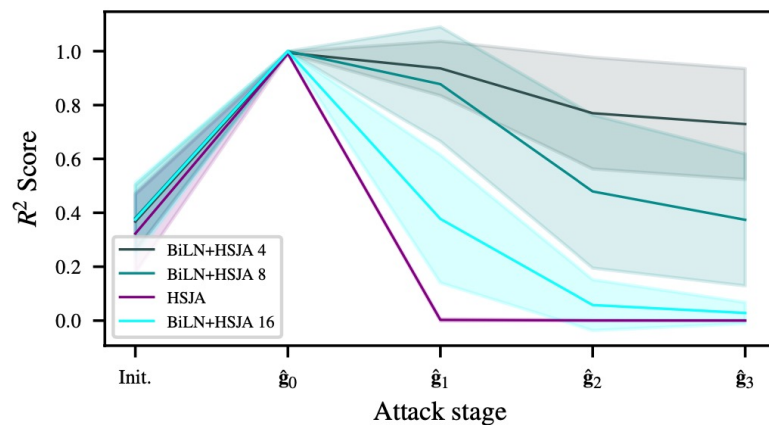
Lower dimension



## A2. Dimension-reduction leads to finer-grained structural information:



## A2. Dimension-reduction leads to finer-grained structural information:



	Attack Variant	$\bar{R}^2$	FID	SR@40k ( $\epsilon=0.031$ )	LPIPS
Madry CIFAR-10	HSJA	0.259	0.244	0.272	0.676±0.275
	→ BiLN 16	0.363	0.074	<b>0.298</b>	0.654±0.277
	→ BiLN 8	0.624	0.026	0.224	0.668±0.304
	→ BiLN 4	<b>0.779</b>	<b>0.026</b>	0.130	0.709±0.345
Natural CIFAR-10	HSJA	0.263	0.240	<b>1.000</b>	0.496±0.211
	→ BiLN 16	0.368	0.085	0.984	0.543±0.227
	→ BiLN 8	0.622	0.028	0.826	0.624±0.253
	→ BiLN 4	<b>0.759</b>	<b>0.012</b>	0.472	0.651±0.297



Second part of original question, what is the worst-case attack analysis?

Formulate adaptive attacks based on Algorithm 1 & 2, denoted MC and DynBiLN (cyan):

CIFAR-10

Attack Variant	FID	SR AUC ( $\epsilon=0.031$ )
HSJA	0.253	0.537
→ <i>BiLN 4</i>	0.026 ↓	0.342
→ <i>BiLN 8</i>	0.023 ↓	0.574 ↑
→ <i>BiLN 16</i>	0.074 ↓	0.720 ↑
MC HSJA	0.213 ↓	0.545 ↑
→ <i>BiLN 4</i>	<b>0.022</b> ↓	0.356
→ <i>BiLN 8</i>	0.026 ↓	0.577 ↑
→ <i>BiLN 16</i>	0.068 ↓	0.705 ↑
→ <i>DynBiLN</i>	0.030 ↓	0.607 ↑
RayS	0.057	<b>1.000</b>

ImageNet

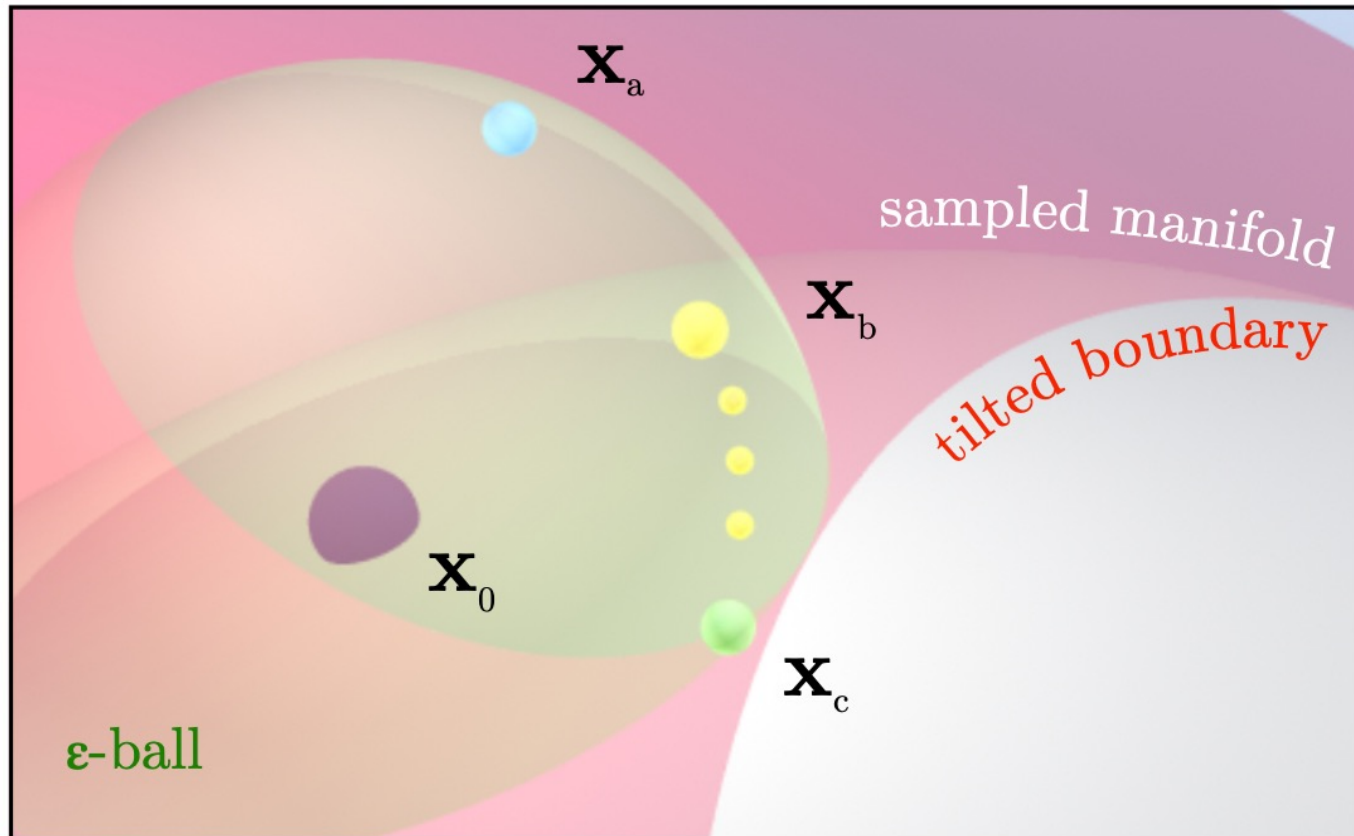
Attack Variant	FID	SR AUC ( $\epsilon=0.031$ )
HSJA	1.541	0.344
→ <i>BiLN 16</i>	0.312 ↓	0.777 ↑
→ <i>BiLN 32</i>	1.085 ↓	0.771 ↑
→ <i>BiLN 64</i>	2.567	0.655 ↑
MC HSJA	1.591	0.331
→ <i>BiLN 16</i>	<b>0.271</b> ↓	0.772 ↑
→ <i>BiLN 32</i>	1.079 ↓	0.771 ↑
→ <i>BiLN 64</i>	2.287	0.615 ↑
→ <i>DynBiLN</i>	0.657 ↓	0.774 ↑
RayS	0.302	<b>1.000</b>







# Geometric Interpretation





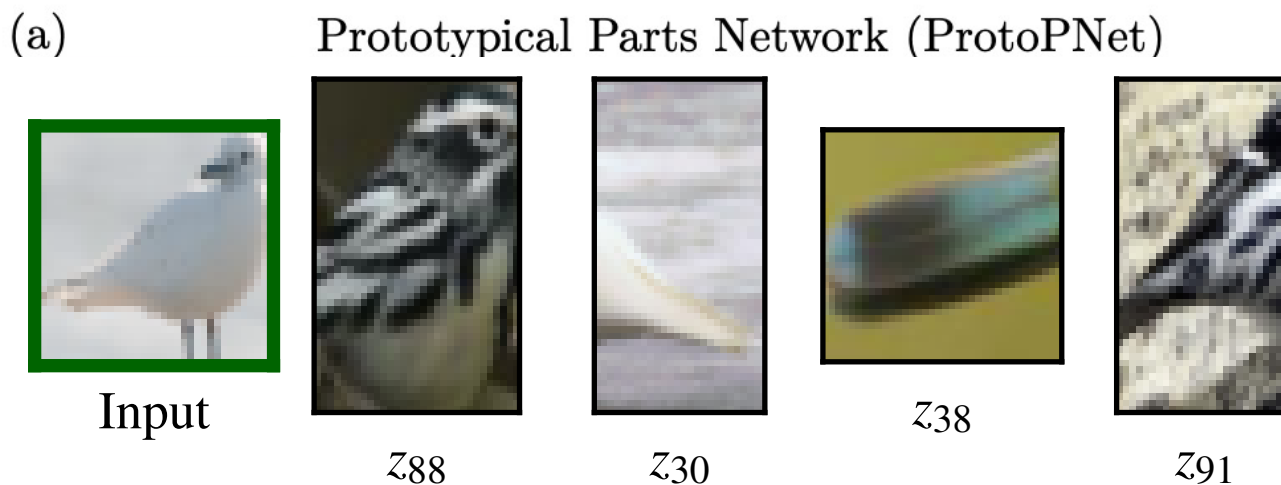
Two main questions:

1. Is agent concept resolution possible from an *adversary's* perspective? What's the worst-case security analysis?
2. It isn't always realistic to have a human-in-the-loop, or fine-grained data labels. What are ways around this?

A1: Expansion of our previous hard-label paper, in submission to IEEE SaTML 2023

A2: We presented an initial idea @ NAACL 2022. Introduced expansion during previous meeting. Then worked on it as part of AFRL 2022 internship.

First, agents learn human-interpretable perceptual knowledge priors:



C. Chen, O. Li, C. Tao, A. J. Barnett, J. Su, and C. Rudin, "This Looks Like That: Deep Learning for Interpretable Image Recognition," *arXiv:1806.10574 [cs, stat]*, 2019.

# Multi-task learning (MTL)

- Sender solves two joint tasks:
  1. Learn to embed their top-1 activate structure ( $\mathbf{z}^S$ ) in the message
  2. Learn to describe the target objects
- Receiver solves two joint tasks:
  1. Learn to reconstruct the sender's top-1 structure ( $rec(\mathbf{z}^S)$ ) from the message (*reconstruction loss*)

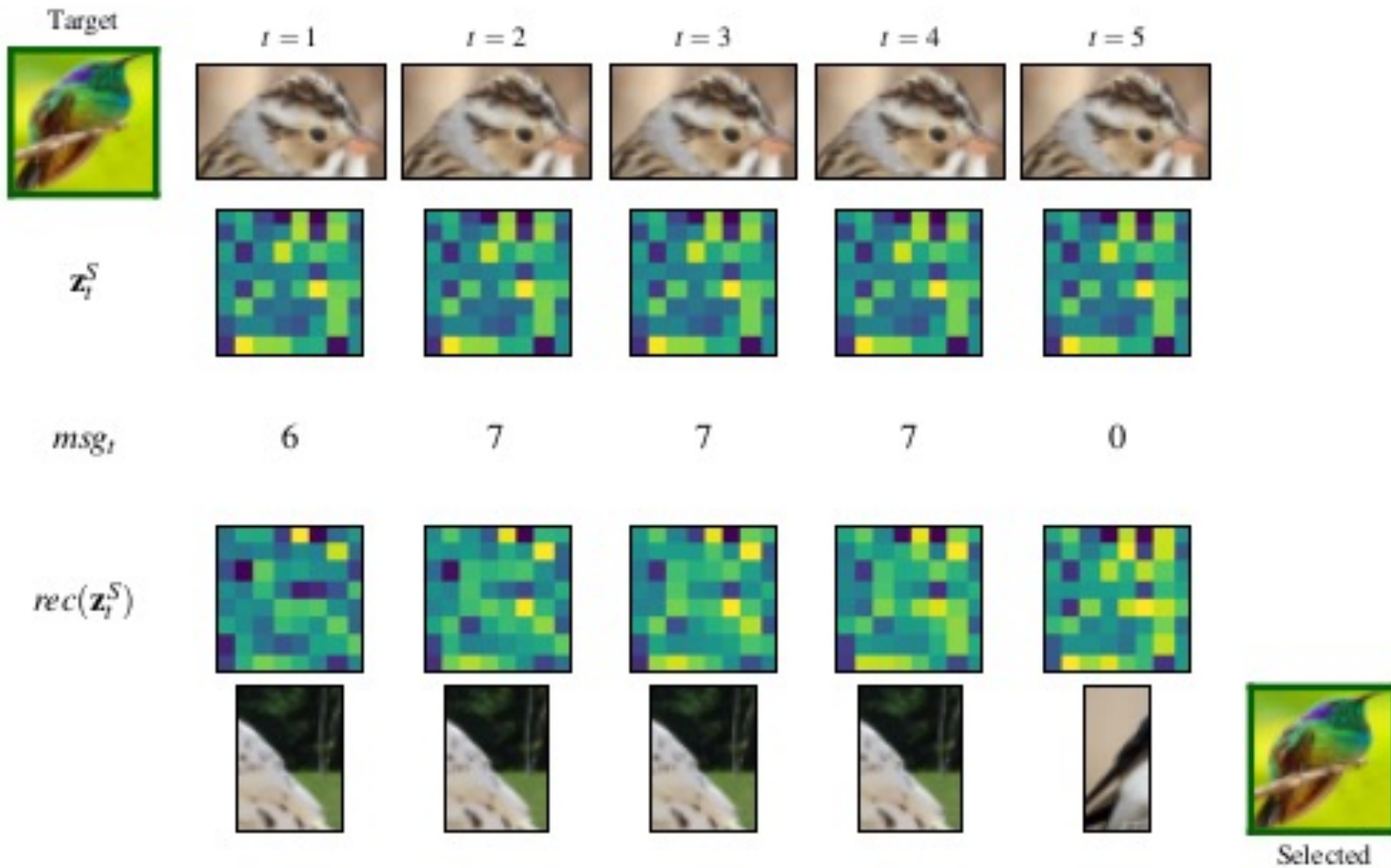
$$\mathcal{L}_{rec}(\mathbf{z}^S, rec(\mathbf{z}^S)) = \frac{1}{L} \sum_{l=1}^L |\mathbf{z}_{(l)}^S - rec(\mathbf{z}_{(l)}^S)|$$

2. Learn to signal the correct target object (*classification loss*)

$$\mathcal{L}_{cls}(\mathbf{t}) = - \sum_{l=1}^L \alpha \log p(y_{(l)} = \mathbf{t} \mid msg_{(l)}).$$

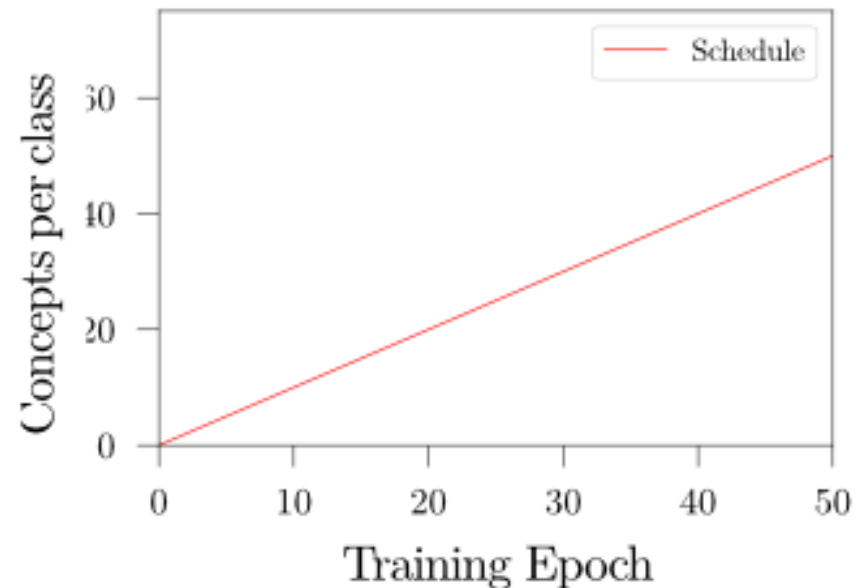
$$\mathcal{L} = \mathcal{L}_{cls} + \mathcal{L}_{rec}$$

# Qualitative Results



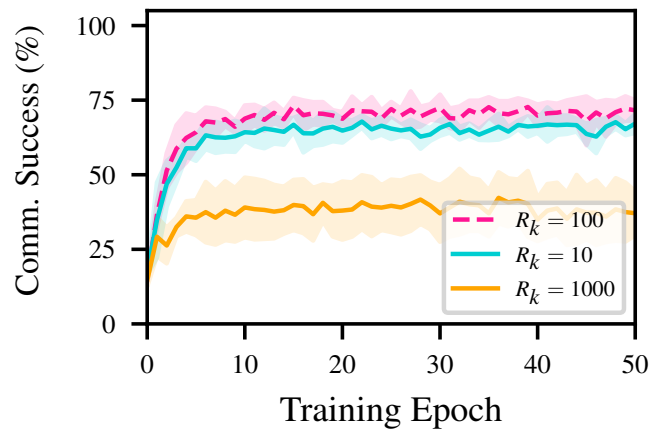
# 'Tatanka' game

Consider a gradual expansion of the sender agent's concept allowance, as in "Tatanka" clip from Dances with Wolves with Wolves:

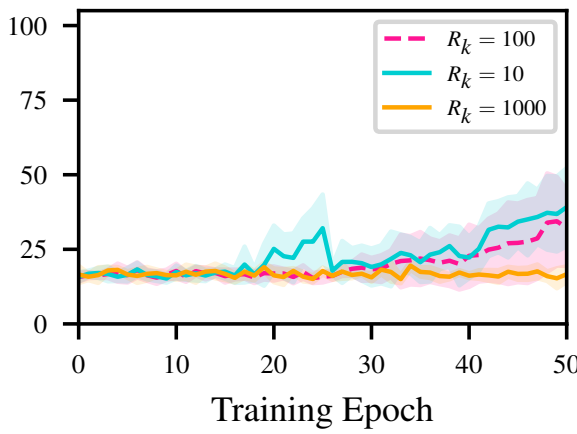




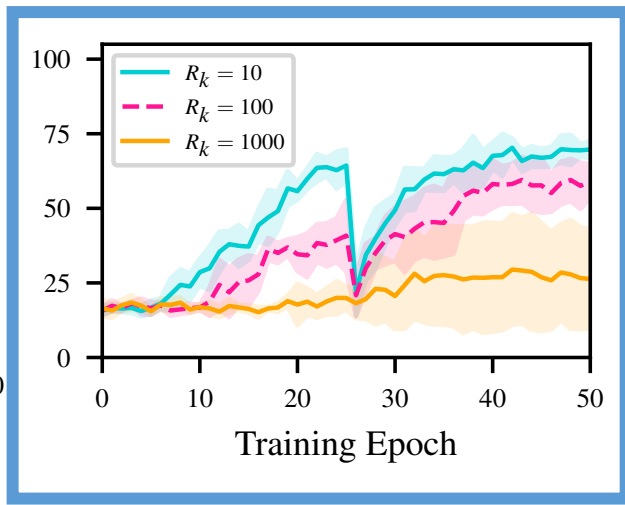
# Concept allowance



Baseline



Reification (Ours)



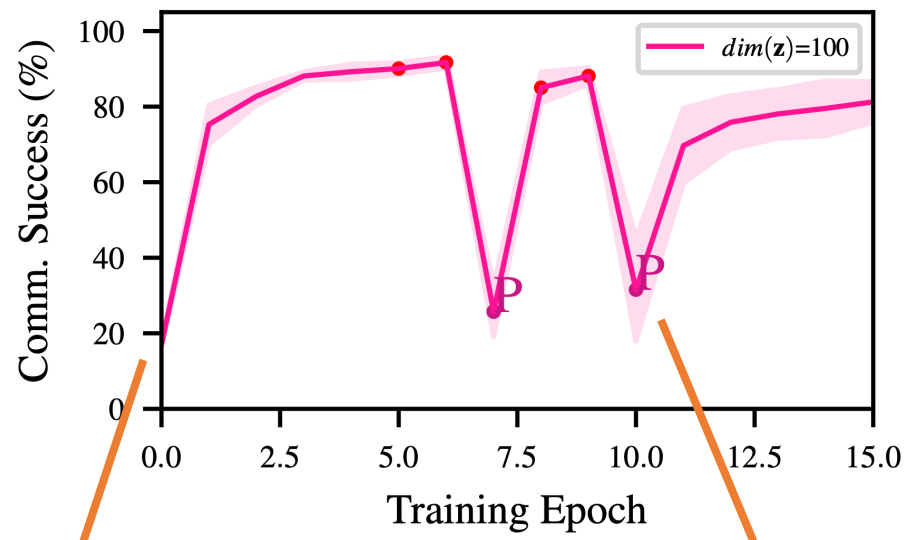
Reification "Tatanka" Variant (Ours)

- Senders solve ~~two~~ **three** joint tasks:
  1. Learn to embed their top-1 activate structure in the message
  2. Learn to describe the target objects
  3. **Update knowledge structure based on embedding difficulty**
- Receivers solve ~~two~~ **three** joint tasks:
  1. Learn to reconstruct the sender's top-1 structure from the message
  2. Learn to signal the correct target object
  3. **Update knowledge structure based on perceived utility of sender structure**

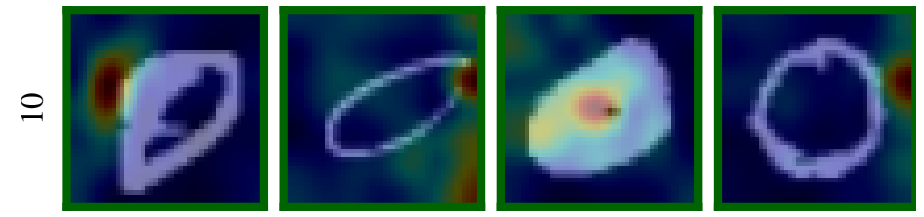
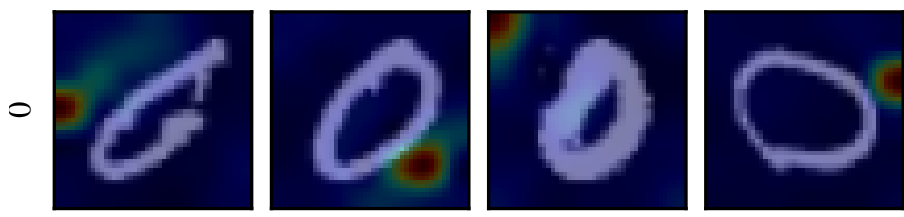




## Training instability and automatic recovery:



P = human-aligned correction





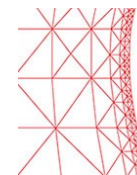
Adversaries can learn semantic structure in a neighborhood around a sample, and this informs geometric interpretation of generalization errors.

- Can we get the global semantic structure with few samples and queries? Implication: leakage of learned manifold
- Connection to diffusion models

Semiotic learning offers an avenue for automatic structural validation, without explicit labels!

Graduation: Dec. 2022

Joining UDRI in January



University of Dayton  
Research Institute



Thank you

w.garcia@ufl.edu

